$L_2(81).2_2 \pmod{5}$

| | blocks | defect | matrix | | blocks | defect | matrix |
|----|--------|--------|---|------|--------|--------|---|
| G: | 1 | 1 | 4×2 | | 41 | 0 | $80_{38} = \chi_{22,1}, \varphi_{22,1}$ |
| | 2 | 1 | 4×2 | | 42 | 0 | $80_{39} = \chi_{23,0}, \varphi_{23,0}$ |
| | 3 | 1 | 5×1 | | 43 | 0 | $80_{40} = \chi_{23,1}, \varphi_{23,1}$ |
| | 4 | 0 | $80_1 = \chi_{4,0}, \varphi_{4,0}$ | | 44 | 1 | 5×1 |
| | 5 | 0 | $80_2 = \chi_{4,1}, \varphi_{4,1}$ | | 45 | 1 | 5×1 |
| | 6 | 0 | $80_3 = \chi_{5,0}, \varphi_{5,0}$ | | 46 | 1 | 5×1 |
| | 7 | 0 | $80_4 = \chi_{5,1}, \varphi_{5,1}$ | | 47 | 1 | 5×1 |
| | 8 | 0 | $80_5 = \chi_{6,0}, \varphi_{6,0}$ | | 48 | 1 | 5×1 |
| | 9 | 0 | $80_6 = \chi_{6,1}, \varphi_{6,1}$ | | 49 | 1 | 5×1 |
| | 10 | 0 | $80_7 = \chi_{7,0}, \varphi_{7,0}$ | | | | |
| | 11 | 0 | $80_8 = \chi_{7,1}, \varphi_{7,1}$ | 2.G: | 50 | 0 | $80_{41} = \chi_{44+}, \varphi_{28+}$ |
| | 12 | 0 | $80_9 = \chi_{8,0}, \varphi_{8,0}$ | | 51 | 0 | $80_{42} = \chi_{46,0}, \varphi_{30,0}$ |
| | 13 | 0 | $80_{10} = \chi_{8,1}, \varphi_{8,1}$ | | 52 | 0 | $80_{43} = \chi_{46,1}, \varphi_{30,1}$ |
| | 14 | 0 | $80_{11} = \chi_{9,0}, \varphi_{9,0}$ | | 53 | 0 | $80_{44} = \chi_{47,0}, \varphi_{31,0}$ |
| | 15 | 0 | $80_{12} = \chi_{9,1}, \varphi_{9,1}$ | | 54 | 0 | $80_{45} = \chi_{47,1}, \varphi_{31,1}$ |
| | 16 | 0 | $80_{13} = \chi_{10,0}, \varphi_{10,0}$ | | 55 | 0 | $80_{46} = \chi_{48,0}, \varphi_{32,0}$ |
| | 17 | 0 | $80_{14} = \chi_{10,1}, \varphi_{10,1}$ | | 56 | 0 | $80_{47} = \chi_{48,1}, \varphi_{32,1}$ |
| | 18 | 0 | $80_{15} = \chi_{11,0}, \varphi_{11,0}$ | | 57 | 0 | $80_{48} = \chi_{49,0}, \varphi_{33,0}$ |
| | 19 | 0 | $80_{16} = \chi_{11,1}, \varphi_{11,1}$ | | 58 | 0 | $80_{49} = \chi_{49,1}, \varphi_{33,1}$ |
| | 20 | 0 | $80_{17} = \chi_{12,0}, \varphi_{12,0}$ | | 59 | 0 | $80_{50} = \chi_{50,0}, \varphi_{34,0}$ |
| | 21 | 0 | $80_{18} = \chi_{12,1}, \varphi_{12,1}$ | | 60 | 0 | $80_{51} = \chi_{50,1}, \varphi_{34,1}$ |
| | 22 | 0 | $80_{19} = \chi_{13,0}, \varphi_{13,0}$ | | 61 | 0 | $80_{52} = \chi_{51,0}, \varphi_{35,0}$ |
| | 23 | 0 | $80_{20} = \chi_{13,1}, \varphi_{13,1}$ | | 62 | 0 | $80_{53} = \chi_{51,1}, \varphi_{35,1}$ |
| | 24 | 0 | $80_{21} = \chi_{14,0}, \varphi_{14,0}$ | | 63 | 0 | $80_{54} = \chi_{52,0}, \varphi_{36,0}$ |
| | 25 | 0 | $80_{22} = \chi_{14,1}, \varphi_{14,1}$ | | 64 | 0 | $80_{55} = \chi_{52,1}, \varphi_{36,1}$ |
| | 26 | 0 | $80_{23} = \chi_{15,0}, \varphi_{15,0}$ | | 65 | 0 | $80_{56} = \chi_{53,0}, \varphi_{37,0}$ |
| | 27 | 0 | $80_{24} = \chi_{15,1}, \varphi_{15,1}$ | | 66 | 0 | $80_{57} = \chi_{53,1}, \varphi_{37,1}$ |
| | 28 | 0 | $80_{25} = \chi_{16,0}, \varphi_{16,0}$ | | 67 | 0 | $80_{58} = \chi_{54,0}, \varphi_{38,0}$ |
| | 29 | 0 | $80_{26} = \chi_{16,1}, \varphi_{16,1}$ | | 68 | 0 | $80_{59} = \chi_{54,1}, \varphi_{38,1}$ |
| | 30 | 0 | $80_{27} = \chi_{17,0}, \varphi_{17,0}$ | | 69 | 0 | $80_{60} = \chi_{55,0}, \varphi_{39,0}$ |
| | 31 | 0 | $80_{28} = \chi_{17,1}, \varphi_{17,1}$ | | 70 | 0 | $80_{61} = \chi_{55,1}, \varphi_{39,1}$ |
| | 32 | 0 | $80_{29} = \chi_{18,0}, \varphi_{18,0}$ | | 71 | 0 | $80_{62} = \chi_{56,0}, \varphi_{40,0}$ |
| | 33 | 0 | $80_{30} = \chi_{18,1}, \varphi_{18,1}$ | | 72 | 0 | $80_{63} = \chi_{56,1}, \varphi_{40,1}$ |
| | 34 | 0 | $80_{31} = \chi_{19,0}, \varphi_{19,0}$ | | 73 | 0 | $80_{64} = \chi_{57,0}, \varphi_{41,0}$ |
| | 35 | 0 | $80_{32} = \chi_{19,1}, \varphi_{19,1}$ | | 74 | 0 | $80_{65} = \chi_{57,1}, \varphi_{41,1}$ |
| | 36 | 0 | $80_{33} = \chi_{20,0}, \varphi_{20,0}$ | | 75 | 0 | $80_{66} = \chi_{58,0}, \varphi_{42,0}$ |
| | 37 | 0 | $80_{34} = \chi_{20,1}, \varphi_{20,1}$ | | 76 | 0 | $80_{67} = \chi_{58,1}, \varphi_{42,1}$ |
| | 38 | 0 | $80_{35} = \chi_{21,0}, \varphi_{21,0}$ | | 77 | 0 | $80_{68} = \chi_{59,0}, \varphi_{43,0}$ |
| | 39 | 0 | $80_{36} = \chi_{21,1}, \varphi_{21,1}$ | | 78 | 0 | $80_{69} = \chi_{59,1}, \varphi_{43,1}$ |
| | 40 | 0 | $80_{37} = \chi_{22,0}, \varphi_{22,0}$ | | 79 | 0 | $80_{70} = \chi_{60,0}, \varphi_{44,0}$ |
| 1 | l | I | 1 , , , , , , , , , , , , , , , , , , , | | 80 | 0 | $80_{71} = \chi_{60,1}, \varphi_{44,1}$ |

| blocks | defect | matrix |
|--|--------------------------------------|---|
| 81 82 83 84 85 86 87 88 | 0 0 0 0 0 0 0 0 | $80_{72} = \chi_{61,0}, \varphi_{45,0}$ $80_{73} = \chi_{61,1}, \varphi_{45,1}$ $80_{74} = \chi_{62,0}, \varphi_{46,0}$ $80_{75} = \chi_{62,1}, \varphi_{46,1}$ $80_{76} = \chi_{63,0}, \varphi_{47,0}$ $80_{77} = \chi_{63,1}, \varphi_{47,1}$ $80_{78} = \chi_{64,0}, \varphi_{48,0}$ $80_{79} = \chi_{64,1}, \varphi_{48,1}$ $80_{80} = \chi_{65,0}, \varphi_{49,0}$ |

| blocks | defect | matrix |
|----------------------------------|----------------------------|--|
| 90 91 92 93 94 95 | 0 1 1 1 1 1 | $80_{81} = \chi_{65,1}, \varphi_{49,1}$ 5×1 |
| 96 97 98 | 1 1 1 | 5×1 5×1 5×1 |

| Block 1: | $\varphi_{1,0}$ | $\varphi_{24,1}$ |
|----------------------|-----------------|------------------|
| $1_1 = \chi_{1,0}$ | 1 | |
| $81_2 = \chi_{24,1}$ | | 1 |
| $82_4 = \chi_{26,0}$ | 1 | 1 |
| $82_6 = \chi_{27,0}$ | 1 | 1 |

$$\begin{array}{rcl} \varphi_{1,0} & = & 1_1 \\ \varphi_{24,1} & = & 81_2 \end{array}$$

Block 2:

$$\varphi_{1,1}$$
 $\varphi_{24,0}$
 $1_2 = \chi_{1,1}$
 1
 .

 $81_1 = \chi_{24,0}$
 .
 1

 $82_5 = \chi_{26,1}$
 1
 1

 $82_7 = \chi_{27,1}$
 1
 1

$$\begin{array}{rcl} \varphi_{1,1} & = & 1_2 \\ \varphi_{24,0} & = & 81_1 \end{array}$$

Block 3:
$$\varphi_{2+}$$

$$82_1 = \chi_{2+} \qquad 1$$

$$82_{12} = \chi_{30,0} \qquad 1$$

$$82_{13} = \chi_{30,1} \qquad 1$$

$$82_{14} = \chi_{31,0} \qquad 1$$

$$82_{15} = \chi_{31,1} \qquad 1$$

$$\varphi_{2+} = 82_1$$

| Block 44: | $\varphi_{25,0}$ | | | |
|-------------------------|------------------|------------------|---|----------|
| $82_2 = \chi_{25,0}$ | 1 | | | |
| $82_{16} = \chi_{32,0}$ | 1 | $\varphi_{25,0}$ | = | 82_{2} |
| $82_{18} = \chi_{33,0}$ | 1 | , -,- | | |
| $82_{21} = \chi_{34,1}$ | 1 | | | |
| $82_{23} = \chi_{35,1}$ | 1 | | | |

| Block 45: | $\varphi_{25,1}$ | |
|---|------------------|-------------------------|
| $82_3 = \chi_{25,1}$ | 1 | |
| $82_{17} = \chi_{32,1}$ | 1 | $\varphi_{25,1} = 82_3$ |
| $82_{19} = \chi_{33,1}$ | 1 | . , |
| $82_{20} = \chi_{34,0}$ | 1 | |
| $82_{22} = \chi_{35,0}$ | 1 | |
| $82_{22} = \chi_{34,0}$ $82_{22} = \chi_{35,0}$ | 1 | |

| Block 46: | $\varphi_{26,0}$ | | | |
|-------------------------|------------------|------------------|---|--|
| $82_8 = \chi_{28,0}$ | 1 | | | |
| $82_{24} = \chi_{36,0}$ | 1 | $\varphi_{26,0}$ | = | |
| $82_{27} = \chi_{37,1}$ | 1 | , | | |
| $82_{37} = \chi_{42,1}$ | 1 | | | |
| $82_{38} = \chi_{43,0}$ | 1 | | | |

| Block 47: | $\varphi_{26,1}$ | | | |
|-------------------------|------------------|------------------|---|----|
| $82_9 = \chi_{28,1}$ | 1 | | | |
| $82_{25} = \chi_{36,1}$ | 1 | $\varphi_{26,1}$ | = | 82 |
| $82_{26} = \chi_{37,0}$ | 1 | , | | |
| $82_{36} = \chi_{42,0}$ | 1 | | | |
| $82_{39} = \chi_{43,1}$ | 1 | | | |

| Block 48: | $\varphi_{27,0}$ |
|-------------------------|------------------|
| $82_{10} = \chi_{29,0}$ | 1 |
| $82_{28} = \chi_{38,0}$ | 1 |
| $82_{31} = \chi_{39,1}$ | 1 |
| $82_{32} = \chi_{40,0}$ | 1 |
| $82_{35} = \chi_{41,1}$ | 1 |

| Block 49: | $\varphi_{27,1}$ | | | |
|-------------------------|------------------|------------------|---|---|
| $82_{11} = \chi_{29,1}$ | 1 | | | |
| $82_{29} = \chi_{38,1}$ | 1 | $\varphi_{27,1}$ | = | 8 |
| $82_{30} = \chi_{39,0}$ | 1 | , | | |
| $82_{33} = \chi_{40,1}$ | 1 | | | |
| $82_{34} = \chi_{41,0}$ | 1 | | | |
| | | | | |

| Block 91: | $arphi_{50,0}$ | | | |
|-------------------------|----------------|------------------|---|---|
| $82_{40} = \chi_{66,0}$ | 1 | | | |
| $82_{48} = \chi_{70,0}$ | 1 | $\varphi_{50,0}$ | = | į |
| $82_{63} = \chi_{77,1}$ | 1 | , | | |
| $82_{67} = \chi_{79,1}$ | 1 | | | |
| $82_{77} = \chi_{84,1}$ | 1 | | | |
| | 1 | | | |

| Block 92: | $arphi_{50,1}$ | | | |
|-------------------------|----------------|------------------|---|---|
| $82_{41} = \chi_{66,1}$ | 1 | | | |
| $82_{49} = \chi_{70,1}$ | 1 | $\varphi_{50,1}$ | = | 8 |
| $82_{62} = \chi_{77,0}$ | 1 | ,, | | |
| $82_{66} = \chi_{79,0}$ | 1 | | | |
| $82_{76} = \chi_{84,0}$ | 1 | | | |

| Block 93: | $\varphi_{51,0}$ | | | |
|---|------------------|----------------|---|------------------|
| $82_{42} = \chi_{67,0}$ $82_{50} = \chi_{71,0}$ $82_{61} = \chi_{76,1}$ $82_{64} = \chi_{78,0}$ $82_{78} = \chi_{85,0}$ | 1 1 1 1 | $arphi_{51,0}$ | = | 82 ₁₀ |

| $\begin{array}{c cccc} 22_{51} = \chi_{71,1} & 1 & \varphi_{51,1} & = \\ 22_{60} = \chi_{76,0} & 1 & & \\ 22_{65} = \chi_{78,1} & 1 & & & \end{array}$ | Block 94: | $\varphi_{51,1}$ | | |
|--|-------------------------|------------------|------------------|---|
| $\begin{array}{c c} 2_{60} = \chi_{76,0} & 1\\ 2_{65} = \chi_{78,1} & 1 \end{array}$ | $82_{43} = \chi_{67,1}$ | 1 | | |
| $22_{65} = \chi_{78,1}$ 1 | $82_{51} = \chi_{71,1}$ | 1 | $\varphi_{51,1}$ | = |
| | $82_{60} = \chi_{76,0}$ | 1 | , | |
| $22_{79} = \chi_{85,1}$ 1 | $82_{65} = \chi_{78,1}$ | 1 | | |
| | $82_{79} = \chi_{85,1}$ | 1 | | |

| Block 95: | $\varphi_{52,0}$ | |
|-------------------------|------------------|----------------------------|
| $82_{44} = \chi_{68,0}$ | 1 | |
| $82_{52} = \chi_{72,0}$ | 1 | $\varphi_{52,0} = 82_{12}$ |
| $82_{57} = \chi_{74,1}$ | 1 | . , |
| $82_{71} = \chi_{81,1}$ | 1 | |
| $82_{74} = \chi_{83,0}$ | 1 | |

| Block 96: | $arphi_{52,1}$ | | | |
|-------------------------|----------------|------------------|---|----|
| $82_{45} = \chi_{68,1}$ | 1 | | | |
| $82_{53} = \chi_{72,1}$ | 1 | $\varphi_{52,1}$ | = | 82 |
| $82_{56} = \chi_{74,0}$ | 1 | ,- | | |
| $82_{70} = \chi_{81,0}$ | 1 | | | |
| $82_{75} = \chi_{83,1}$ | 1 | | | |

| $\begin{array}{c cccc} 82_{46} = \chi_{69,0} & 1 \\ 82_{54} = \chi_{73,0} & 1 \\ 82_{58} = \chi_{75,0} & 1 \\ 82_{68} = \chi_{80,0} & 1 \end{array}$ |
|--|
| $82_{58} = \chi_{75,0} \qquad 1$ |
| |
| $82_{68} = \chi_{80,0}$ 1 |
| |

| Block 98: | $arphi_{53,1}$ | | | | |
|-------------------------|----------------|--------------|-----|---|-----------|
| $82_{47} = \chi_{69,1}$ | 1 | | | | |
| $82_{55} = \chi_{73,1}$ | 1 | $arphi_{53}$ | 3,1 | = | 82_{15} |
| $82_{59} = \chi_{75,1}$ | 1 | | _ | | |
| $82_{69} = \chi_{80,1}$ | 1 | | | | |
| $82_{73} = \chi_{82,1}$ | 1 | | | | |
| | | | | | |