We state some recent results on the structure of subalgebras of the three classical simple Lie algebras sl_{∞} , so_{∞} , and sp_{∞} . In particular we give a characterization of Levi components of parabolic subalgebras of these algebras.