Specht modules play an important role in the representation theory of the symmetric group \mathfrak{S}_n . Over fields of characteristic 0 they are precisely the simple \mathfrak{S}_n -modules; over fields of positive characteristic this is no longer true, and many basic questions about their structure are not answered. In this talk, I will discuss some homological properties of Specht modules over fields of characteristic p > 0, by showing where Specht modules in wild p-blocks of small defect occur in the Auslander-Reiten quiver. This is joint work with K. Erdmann.